

# I. Classical Mechanics

1. **Newton's laws of motion:** equations of motion for a particle, superposition.
2. **Central force problem:** reduction to a 1-D problem, Newton's universal law of gravitation, gravitational potential, Keplerian orbits.
3. **Reference frames:** transformations between moving observers, transformations to rotating frames, special relativity, relativistic momentum and energy, relativistic form of Newton's law.
4. **Elastic and inelastic collisions:** conservation of energy and momentum, Rutherford scattering, hard-sphere scattering, scattering cross sections.
5. **Dynamics of a system of particles:** center-of-mass, moment of inertia, rotational kinetic energy, linear and angular momentum of a system, Newton's laws in angular form, collisions involving rotation.
6. **Dynamics of rigid bodies:** inertia tensor, principal axes, Euler angles, Euler's equations for a rigid body, free motion of a symmetric top.
7. **Oscillations:** simple harmonic oscillator, damped oscillations, transients and steady-state oscillations with a harmonic driving force, superposition, Fourier series, nonlinear oscillations.
8. **Coupled oscillators:** weak coupling, general coupled oscillations, normal modes and normal coordinates, superposition.
9. **Dynamics of continuous media:** the wave equation, generic solutions, phase velocity, group velocity, wave packets, dispersion, coupling to discrete oscillators, standing waves, reflection and transmission, refraction.
10. **Statics:** conditions for equilibrium, stability and metastability, small oscillations in presence of a perturbation.
11. **Hamilton's principle:** the action, Lagrange's equation of motion, Lagrange's equations with constraints.
12. **Hamilton's equations of motion:** Hamiltonian form of conservation laws, Poisson brackets.
13. **Canonical transformations:** canonical coordinates, generating functions.
14. **Hamilton-Jacobi method:** Hamilton's principle function, Hamilton's characteristic function, action-angle variables.

## II. Electromagnetism

1. **Electrostatics:** Coulomb's force law, Gauss's law, electric potential, superposition, boundary conditions for conductors, the method of images, Greens functions solutions, the dipole field and multipole expansion.
2. **Electric fields in dielectrics:** polarization, electric displacement, linear dielectrics, boundaries between different dielectrics.
3. **Magnetostatics:** the Lorentz force law, Biot-Savart law, Ampere's law, the vector potential, boundary conditions for conductors.
4. **Magnetic fields in matter:** magnetization, magnetic field H, linear magnetic materials, ferromagnets, superconductors.
5. **Electrodynamics:** Faraday's law for magnetic induction, Maxwell's equations, classes of boundary conditions, energy density and the Poynting vector, momentum flow.
6. **Gauge symmetry:** gauge transformations and gauge invariance.
7. **Electromagnetic waves:** in vacuum, in dielectric media, in conductors, polarization, reflection and refraction at a plane interface.
8. **Standing waves:** modes in a cavity, wave guides, optical fibers.
9. **Radiation and scattering:** electric and magnetic dipole radiation, scattering by a harmonically bound charge.
10. **Diffraction:** single-slit and double-slit diffraction, interferometers, Gaussian beams, diffraction-limited optics.
11. **Frame transformations:** fields in rotating frames, Lorentz transformation of fields, the electromagnetic field tensor, boosting of E and B fields.
12. **Interactions of charges with fields:** free motion of charges in external fields, forces on current-carrying conductors, forces on dielectrics.

### III. Statistical Physics

1. **Thermodynamics:** quasistatic processes, reversible and irreversible processes, first and second laws of thermodynamics, entropy.
2. **Forms of energy:** heat and work, internal energy, Helmholtz and Gibbs free energies, enthalpy, Legendre transformations between forms.
3. **Intrinsic state variables:** temperature, pressure, chemical potential, chemical equilibrium, spontaneous processes.
4. **The ideal gas:** Maxwellian velocity distribution, dilute gas partition function, heat capacities for different molecular classes, the equation of state.
5. **Heat engines and refrigerators:** efficiency of a cycle, Carnot engines and maximal efficiency allowed by second law.
6. **Phase transitions:** equations of state, first-order phase transitions, phase diagrams, equilibrium phase co-existence.
7. **Statistical ensembles:** microcanonical, canonical, grand canonical, meaning of temperature, partition functions for each ensemble, equipartition theorem, meaning of entropy.
8. **State counting:** Boltzmann statistics, the Boltzmann factor, state counting with identical particles, the Gibbs factor, Bose statistics, Fermi statistics.
9. **Blackbody radiation:** Rayleigh-Jeans law, Stefan-Boltzmann law, Planck's hypothesis, equation of state of the photon gas, radiated power.
10. **Paramagnetism:** the classical spin system, the Ising model of ferromagnetism (mean field).
11. **Fermi gas:** density of states, partition function, pressure, chemical potential.
12. **Debye theory of solids:** heat capacity, the phonon gas.
13. **Transport coefficients:** mean free path, viscosity, thermal conductivity, diffusion in a dilute gas, electrical conductivity in a conductor.
14. **Fluctuations:** the random walk, Brownian motion, electrical noise in a circuit.
15. **Non-ideal gas:** scattering effects, time evolution of phase-space density, Boltzmann equation, equation of state of non-ideal gas.

# Quantum Mechanics

1. **State vectors and observables:** the Hilbert space, Hermetian operators, commutation relations, completeness relations, eigenvalues and eigenstates, expectation values, projection and quantum measurement.
2. **Two-state problems:** raising and lowering operators, commutation relations, quantum oscillations, the ammonia molecule.
3. **Free particle motion:** Gaussian wave packets, continuum state normalization, de-Broglie and Compton wavelengths, the Heisenberg uncertainty principle, meaning of the wave function, particle interference.
4. **Angular momentum:** angular momentum algebra, addition rules, spin, spinors and spin-1/2, Pauli matrices, state counting, degeneracy.
5. **Bound states in 1-D:** the time-independent Schrodinger equation, the infinite square well and finite square well, barrier penetration and tunneling, the simple harmonic oscillator, raising and lowering operator formulation.
6. **Bound states in 3-D:** reduction to 1-D for central potentials, spherical harmonics, 3-D harmonic oscillator, the hydrogen atom, radial wave function solutions for spherical well, fine and hyperfine corrections for the hydrogen atom.
7. **Approximate methods:** time-independent perturbation theory, the WKB approximation, variational methods, Bohr-Sommerfeld quantization condition.
8. **Symmetries:** symmetry transformations and unitary operators, Noether's theorem, continuous symmetries, discrete symmetries.
9. **Motion in an external field:** gauge transformations, Landau levels in an external magnetic field, magnetic resonances.
10. **Scattering states:** general form for in-states, out-states, elastic scattering amplitude, the partial wave expansion, phase shifts, scattering length, effective range, resonances, the Froissart bound.
11. **Elementary scattering theory:** the S matrix, the Lipmann-Schwinger equation, the T matrix, the optical theorem, the Born approximation, dispersion relations.
12. **Time-dependent problems:** Schrodinger and Heisenberg equations of motion, time-dependent perturbation theory, Fermi's golden rule, metastability and decay, electric dipole transition rates.
13. **Identical Particles:** creation and annihilation operators, bosonic and fermionic commutation relations, state counting in systems of multiple fermions, bosons, coherent states.
14. **Relativistic quantum mechanics:** the Dirac equation, free solutions, negative energy states and antiparticles, non-relativistic reduction, zitterbewegung.